



The equation $y=x^2$ is symmetric or invariant under the transformation A, i.e. it looks the same before and after the transformation.

- Moder quantum field theories are gauge invariant theories i.e. they are theories were the main equations do not change when a gauge transformation is performed.
- By requiring that the theories are gauge invariant one can in fact deduce the various interactions.

What is a gauge transformation?

- There are several forms of gauge transformations corresponding to different interactions.
- As an example we can look at non-relativistic electromagnetism and start by assuming that the equation of motion for a free non-relativist particle is:

$$i\frac{\partial \psi(\vec{x},t)}{\partial t} = -\frac{1}{2m}\nabla^2 \psi(\vec{x},t)$$

The free particle Schroedinger equation

 Assume that we want to modify this equation so that it also describes particles that interact electromagnetically.

Assume further that we know that the new equation has to be invariant under a so-called U(1) phase transformation:

$$\psi(\vec{x},t) \to \psi'(\vec{x},t) = e^{iq\alpha(\vec{x},t)}\psi(\vec{x},t)$$

were $\alpha(\dot{x}, t)$ is an arbitrary continous function.

• However, if we try to put the transformed wavefunction $\psi'(\vec{x}, t)$ into the Schroedinger equation we discover that it is not a solution.



In order to keep the invariance condition satisfied it is necessary to add a minimal field to the Schroedinger equation, i.e., an interaction will have to be introduced.

The interaction is introduced by requiring that the Schroedinger equation is also invariant under a gauge transformation of type:

$$\overline{A} \to \overline{A}' = \overline{A} + \nabla \alpha$$
$$V \to V' = V - \frac{\partial \alpha}{\partial t}$$

where A and V are the vector and scalar potenials of the electromagnetic field in which a particle with a charge q is moving.

In order for the free-particle Schroedinger equation to be invariant under both the U(1) phase transformation and the gauge transformation, the equation has to be changed to:

$$i\frac{\partial \Psi(\vec{x},t)}{\partial t} = \left[\frac{1}{2m}(\bar{p}-q\bar{A})+qV\right]\Psi(\vec{x},t)$$

The equation for a non-relativistic particle with charge q moving in an electromagnetic field.

- Glashow, Weinberg and Salam formulated in the sixties a unified theory for the weak and electromagnetic interactions - The electro weak theory.
 - This is a quantum field theory and the details is beyond the scope of this course. We will, however, study some of the predictions of the theory and how these have been tested experimentally.
 - The theory introduces weak isospin charge (I_3^W) and weak hypercharge (Y^W) that are related to electric charge (Q) by $Q = I_3^W + Y^W/2$
 - It also introduces massless gauge particles (W⁺, W⁻, W⁰, B⁰) that interacts with massless fermions in order to make the theory gauge-invariant.

V. Hedberg

- A new field called the Higgs field is introduced in the theory to generate mass to the gauge bosons and the fermions.
- While W⁺ and W⁻ are the well-known bosons responsible for weak radioactive decay, the W⁰ and B⁰ bosons are not observed experimentally. Instead the gauge boson for the electromagnetic interaction (the photon) and the gauge boson for the weak neutral current interaction (the Z⁰) are linear combinations of W⁰ and B⁰:

$$\gamma = B^{0} \cos \theta_{W} + W^{0} \sin \theta_{W}$$
$$Z^{0} = -B^{0} \sin \theta_{W} + W^{0} \cos \theta_{W}$$

• The weak mixing angle (θ_W) is a parameter that is not predicted by the theory but has to be determined experimentally.

V. Hedberg

The theory would lead to infinities if weak interactions could only take place by W-exchange due to divergent processes:



Non-divergent integrals



Divergent integrals

The Z⁰-boson fixes this problem beacuse the addition of its diagrams cancel out the divergencies:



Non-divergent integrals



Divergent integrals

- Two new coupling constants (g_W and g_Z) are introduced in addition to the electric charge (e) that is used in QED and g_s in QCD.
- The coupling constants at the W-, Z- and γ-vertices cannot be independent from each other in order for all the infinities to cancel out in the electroweak theory:

 $e/\sqrt{8} = g_W \sin \theta_W = g_Z \cos \theta_W$ The unification condition.

(alternatively $e = g \sin \theta_W = g \cos \theta_W$ with $g = \sqrt{8} g_W$ and $g' = \sqrt{8} g_Z$)

• The weak mixing angle, or Weinberg angle, is given by: $\cos \theta_W = \frac{M_W}{M_Z}$

• Strength parameters can also be introduced for all interactions: $QED: \alpha = \frac{e^2}{4\pi} \approx \frac{1}{137}$ $QCD: \alpha_s = \frac{g_s^2}{4\pi} \approx \frac{1}{9}$ $EW: \alpha_W = \frac{g_W^2}{4\pi} \approx \frac{1}{250}$ $\alpha_Z = \frac{g_Z^2}{4\pi} \approx \frac{1}{850}$

- The strength parameters can be used to estimate the contribution from different processes (diagrams) to the cross-section.
- As an example one can take muon-scattering on electrons $v_{\mu} + e^- \rightarrow \mu^- + v_e$ for which diagrams with increasing complexity can contribute:



• The second order diagram give a contribution to the cross section that is proportional to a_W^2 and the sixth order diagram a contribution proportional to a_W^6 .

V. Hedberg

Point-like interactions

- Before the electroweak theory, there was Fermi's theory for weak interactions that assumed four-fermion point-like interactions without W and Z exchange.
- Since W bosons are heavy, charged current interactions can be approximated by a zero-range interaction at low energy e.g.



• The strength of the zero-range interaction was given by the Fermi coupling constant (G_F) which is related to g_W by

$$\frac{G_F}{\sqrt{2}} = \frac{g_W^2}{M_W^2} = \frac{4\pi\alpha_W}{M_W^2}$$

where α_W is a weak strength parameter analogous to α in electromagnetic interactions.

A bit of algebra:



• If one then introduces a neutral current coupling constant (G_Z) in the low energy zero-range approximation also, one has:

$$\frac{G_Z}{\sqrt{2}} = \frac{g_Z^2}{M_Z^2} \quad \text{which gives} \quad \frac{G_Z}{G_F} = \frac{\sqrt{2}g_Z^2}{\sqrt{2}g_W^2}M_Z^2 = \frac{\frac{\pi\alpha}{2\cos^2\theta_W}}{\frac{\pi\alpha}{2\sin^2\theta_W}}\cos^2\theta_W = \sin^2\theta_W$$

One could use the relationship G_Z/G_W=sin²(θ_W) together with measurements of weak interaction rates at low energy, i.e. G_Z and G_F, to determine that

 $\sin^2 \theta_W = 0,277 \pm 0,014$

This measurement of the weak mixing angle made it possible to predict the masses of the W and Z:

> $M_W = 78,3 \pm 2,4 \text{ GeV/c}^2$ $M_Z = 89,0 \pm 2,0 \text{ GeV/c}^2$

 It was a strong confirmation that the electroweak theory was correct when the W and Z bosons were later discovered at CERN with the masses predicted from these low energy experiments.

- Today the most precise estimation of the Weinberg angle using many experiments is: $\sin^2 \theta_W = 0.2255 \pm 0.0021$
- Putting these values into the previous formulas give: $M_W = 78,5 \text{ GeV/c}^2$ $M_Z = 89,0 \text{ GeV/c}^2$ while direct measurements give $M_W = 80,4 \text{ GeV/c}^2$ $M_Z = 91,2 \text{ GeV/c}^2$
- The reason for the difference is that higher-order diagrams, such as those below, were not taken into account in the low-energy formulas:
 vµ
 <



Weak Interactions

W

·νe

b

Since the top-quark is involved in these higher-order corrections, the measurement of electroweak processes could again be used to predict the top-quark mass before it had been discovered:

 $m_t = 170 \pm 30 \text{ GeV/c}^2$

The directly measured mass of the top quark at Fermilab by the CDF experiment gave a value

 $m_t = 176 \pm 5 \, \text{GeV/c}^2$

in perfect agreement with the prediction !

The W and Z bosons

- The force carriers in weak interactions are spin-1 bosons (as in QED and QCD) that couple to quarks and leptons.
 - The force carriers of weak interactions are three intermediate vector bosons: W⁺, W⁻ and Z⁰.
 - Since the W⁺, W⁻ and Z⁰ bosons are very massive particles (m_W=80.4 GeV and M_Z=91.2 GeV) weak interactions have a very short range (order of 2 × 10⁻³ fm).
 - Before the Electroweak Theory was developed, all observed weak processes were charged current reactions (e.g. β-decay) mediated by W⁺ or W⁻ bosons.
 - The Electroweak Theory predicted that neutral current reactions caused by the Z⁰ boson should exist.

Accelerator: The Proton Synchrotron (PS) at CERN

The neutrino beams were created by letting an intense proton beam hit a target. Charged pions and kaons are created in the collision. These decay to neutrinos e.g. π⁺→μ⁺+ν_μ→e⁺+ν_e+ν_μ+ν_μ.





The PS accelerator is 628 m long and has 277 magnets (including 100 dipole bending magnets). It can accelerate protons to 28 GeV.

 Neutral current events was first observed by the Gargamelle experiment at CERN in 1973.



- Step 1. The liquid propane is at a temperature below its boiling point.
- Step 2. When the v enters the propane, its pressure is lowered to make it superheated.
- Step 3. Charged tracks ionize the propane and these ions create bubbles in the liquid.
- Step 4. The bubble tracks are photographed by film cameras.

For more details watch the film at: http://cdsweb.cern.ch/record/43141

One looked for elastic and inelastic neutral current reactions.









• The main background was from neutron - nucleon interactions.



Interpretation of one of the first neutral current reactions seen by the Gargamelle experiment.

V. Hedberg

The accelerator: The Super Proton Synchrotron

 The first study of direct production and decay of the W and Z vector bosons were made by the UA1 and UA2 experiments at the SPS proton-antiproton collider at CERN.





The SPS war originally a 450 GeV fixed target machine but was later converted to a collider with protons colliding with anti-protons. The accelerator is 6.9 km long and has 744 dipole magnets and 216 quadrupol magnets. The acceleration is given by 4 cavities operating at 200 MHz.

• In hadron colliders, the energy of the quarks and gluons that participate in the interaction is only a fraction of the energy of the colliding protons. To produce W- ans Z-bosons with a mass of 80-90 GeV it was therefore necessary to build an accelerator with a beam energy of 270 GeV.



The experiment: UA1



The UA1 detector had a central wire chamber that could measure tracks. A dipole magnet produced a 0.7 T field perpendicular to the beam direction. The electromagnetic calorimeter was of lead/scintillator type and the hadronic was an iron/scintillator sandwich. The muon detector consisted of 8 planes of drift chambers.

V. Hedberg

Production of W and Z bosons

The W and Z bosons are in proton colliders produced by quark-antiquark annihilations:



The lifetime of both the W and the Z is about 3 x 10⁻²⁵ s and particles with such short lifetime are never seen directly in the experiments.

The decay of W and Z bosons

 The W and Z bosons decay in most cases to hadrons but these decays cannot be identified among all the other hadrons created in pp-collisions. Instead one looks for decays to leptons.



EVENT 2958. 1279. Analysis of W-events in UA1

 The analysis was looking for events with a charged lepton and a neutrino.



A high momentum electron is indicated by the arrow.

Transverse momentum



• The transverse momentum and energy of a particle is defined in the following way: $P_T = P \sin(\theta)$ $E_T = E \sin(\theta)$

where θ is the angle to the beam.

- $E_T = P_T$ if the mass of the particle is small since $E^2 = P^2 + m^2$
- The total momentum is zero if the momentum of all the particles in a collision is added up (momentum conservation).
- Neutrinos are, however, not detectable and if the total momentum is different from zero the event is said to have missing momentum (or missing energy).

Analysis of W-events in UA1

• The main selection criteria in the UA1 W-analysis was:

- i) A charged electron or muon with a large momentum (>10 GeV/c);
- ii) This lepton should be emitted at a wide angle to the beam (>5°);
- iii) There should be large missing transverse momentum in the event to indicate neutrino production.



28

Analysis of Z-events in UA1

• The analysis was looking for a pair of charged leptons.



Invariant mass



• The invariant mass of a particle that decays to two other particles can be calculated from the new particles energies and the angle between the two particles:



 $m_{Z}^{2} = (P_{1} + P_{2})^{2}$ (4-vectors)

 $m_{Z}^{2} = 2 E_{1}E_{2} (1 - \cos \varphi)$

Analysis of Z-events in UA1

The main search criteria in the UA1 Z-analysis was to require a pair of charged electrons or muons with a large transverse energy.



V. Hedberg

The accelerator: The Large Electron Positron Collider The LEP accelerator was the largest accelerator ever built. It collided electrons with positrons at four places along a 27 km long tunnel.





The accelerator: LEP





In a first stage the collision energy was equal to the Z mass (91 GeV) but it was increased in a second stage to 209 GeV by installing 288 superconducting cavities. Weak Interactions



V. Hedberg

Weak Interactions

Basic differences between proton and electron colliders.

- The limiting factor for an electron collider is the synchrotron radiation. Total energy loss per turn is proportional to E⁴_{beam}, 1/radius and 1/mass⁴
 i.e the energy loss in an electron machine is 10¹³ times higher than in a proton accelerator.
- 288 superconducting and 56 warm cavities were used at LEP but only 16 cavities are needed at LHC. Accelerating voltage = 3630 MV (LEP) and = 16 MV (LHC)
- The limiting factor for a proton collider is the magnetic field in the dipole bending magnets. The maximum field needed is proportional to Beam momentum
 Length of bending field
- The bending field at LHC (8.38 T) therefore has to be a factor 70 larger than the bending field at LEP (0.12 T).

V. Hedberg

The accelerator: The Large Electron Positron Collider

In an electron-positron collider it is important to know the collision energy with a high accuracy. It took many years to understand the factors that influenced the collision energy in LEP.

Geological shifts



- During 1993 the LEP energy was observed to change with time.
- Part of the change was due to the water level in lake Geneva which caused small geological shifts of the accelerator.
- Rainfalls and the water table in the Jura mountains also affected the LEP energy.




- Earth tides caused by the moon will produce small distortions of the earth's crust.
- This can affect the accelerator so that the electrons orbit change.
- An orbit change of 1 mm will change the energy with about 10 MeV.

Beampipe current

- The trains from Geneva to France caused parasitic currents on the LEP beampipe.
- These currents (1 A) affected the magnetic field in the LEP magnets and this changed the energy.





The DELPHI Experiment

A Time Projection Chamber was used as the main tracking detector.

It was surrounded by an electromagnetic calorimeter sitting inside a solenoid magnet.

The electromagnetic calorimeter had a lead absorbers and a gas detector readout.

The iron return yoke of the magnet had detectors inside it so that it could be used as a hadronic calorimeter.

The muon detector consisted of two driftchamber layers. V. Hedberg



The DELPHI Experiment



The photo shows the DELPHI cavern with the buildings for the electronics hiding the experiment. V. Hedberg Weak Interview



Installation of the large Time Projection Chamber in DELPHI.

Studies of the Z-boson



Studies of the Z-boson



From the number of produced muon pair events one can calculate the cross section for the following process:



Studies of the Z-boson



From the number of produced tau pair events one can calculate the cross section for the following process:



95

 τ^+

1990

1991



V. Hedberg

Weak Interactions

It was possible to determine the partial decay widths of the Z^0 by fitting Breit-Wigners to the measured distributions at LEP.



The height of the peak is proportional to the branching ratios:

V. Hedberg

- The fitted parameters of the Z⁰ peak gave the following result: $M_Z = 91,187 \pm 0,007 \text{ GeV/c}^2$ $\Gamma(Z^0 \rightarrow \text{hadrons}) = 1,741 \pm 0,006 \text{ GeV}$ $\Gamma_Z = 2,490 \pm 0,007 \text{ GeV}$ $\Gamma(Z^0 \rightarrow l^+ l^-) = 0,0838 \pm 0,0003 \text{ GeV}$
- However, the leptonic and hadronic decays account for only 80% of all the Z⁰ decays.
- The remaining decays are those to neutrinos that cannot be measured directly by the experiment since $\Gamma_Z = \Gamma(Z^0 \to \text{hadrons}) + 3\Gamma(Z^0 \to l^+ l^-) + N_V \Gamma(Z^0 \to v_l \overline{v_l})$
- From the measured values of the decay widths one gets

$$N_{v}\Gamma\left(Z^{0} \rightarrow v_{l}\overline{v_{l}}\right) = 0.498 \pm 0.009 \text{ GeV}$$

- The decay rate of the Z⁰ to neutrinos can be calculated: $\Gamma(Z^0 \rightarrow v_l \overline{v_l}) = 0.166 \text{ GeV}$ which together with $N_v \Gamma(Z^0 \rightarrow v_l \overline{v_l}) = 0.498 \text{ GeV}$ gives $N_v = 2.994 \pm 0.011$
- There are no explicit restrictions on the number of generations in the standard model.
- However, the study of the Z⁰ peak at LEP shows that there are only three types of light neutrinos, i.e., with a mass less than M_Z.



The decay of the Z^0 to hadrons and the predictions for different number of neutrino families (N).

Studies of the W-boson

The W bosons were produced in pairs at LEP.





The signature for WW-events was:





A WW-event with 4 jets in the DELPHI experiment.

V. Hedberg

Studies of the W-boson

When the events with WW-pairs had been selected it was possible to calculate the W-mass from the energy and directions of the jets:





The mass distribution from jet-pairs in WW events selected by the DELPHI experiment.

Charged current reactions

- Charged current reactions are reactions mediated by the charged W-bosons. They can be divided up into:
- Purely leptonic processes: $\mu^- \rightarrow e^- + \nu_e + \nu_\mu$ W^{-} $\sim \frac{d}{u} \pi$ $\frac{d}{d}\pi$ W Purely hadronic processes: $\Lambda \rightarrow \pi^- + p$ p W Semileptonic reactions: n $n \rightarrow p + e^{-} + v_{a}$ 50 V. Hedberg Weak Interactions

All the electromagnetic interactions can be built from eight basic interactions:



The basic vertex for electron-photon interactions.

Leptonic weak interaction processes can in a similar way be built from a certain number of reactions corresponding to basic vertices:



It is possible to derive eight basic charged current reactions from the two basic W vertices:



Weak interactions always conserve the lepton numbers: L_{e} , L_{μ} , L_{τ} .

This conservation is guaranteed in Feynman diagrams by:

- at each vertex, there is one arrow pointing in and one out;
- the lepton indices "I" are the same on both lines.



- Leptonic vertices are characterized by the corresponding weak strength parameter, α_W , which do not depend on lepton type.
- The decay rate of W to e+v, can be estimated to first order as $\Gamma(W \rightarrow ev) \approx \alpha_W M_W \approx 80 \alpha_W \text{ GeV}$ since the process only involves one vertex and the lepton masses

since the process only involves one vertex and the lepton masses are negligible.

• A measurement of the decay rate of W to e+v gives $\Gamma(W \rightarrow ev) \approx 0.2 \text{ GeV}$

which translates into an approximative value of $\alpha_W = 0.003$ for the weak strength parameter.

• This is comparable with the value for the electromagnetic strength parameter: α_{em} =0.007 .

- Why is the weak interaction so weak if α_W and α_{em} is of a similar size ?
- Compare the decay of charged and neutral pions:

Electromagnetic decay



Weak decay



(Lifetime of a real W = 0.0000003×10^{-1} 's)

 CONCLUSION: The apparent weakness of the weak interactions is due to the very large W and Z masses.

Weak Interactions

In weak hadronic interactions, constituent quarks emit or absorb W or Z bosons.

Examples:



Neutron β -decay.



The dominant quark diagrams for Λ decay

ASSUMPTION: Lepton-quark symmetry i.e. corresponding generations of quarks and leptons have identical weak interactions. $\begin{pmatrix} v_e \\ - \end{pmatrix} \leftrightarrow \begin{pmatrix} u \\ d \end{pmatrix} \begin{pmatrix} v_{\mu} \\ u^{-} \end{pmatrix} \leftrightarrow \begin{pmatrix} c \\ s \end{pmatrix} \begin{pmatrix} v_{\tau} \\ \tau^{-} \end{pmatrix} \leftrightarrow \begin{pmatrix} t \\ b \end{pmatrix}$

Interactions will then only take place within a family !





• Experimental tests of the assumption of lepton-quark symmetry.

Some weak reactions should be allowed and some should be forbidden if lepton-quark symmetry is true:

Weak Interactions

- Cabibbo introduced the concept of quark mixing in order to explain the kaon decays.
- According to the quark mixing scheme, d- and s-quarks participate in the weak interactions via the linear combinations:

 $d' = d\cos\theta_{C} + s\sin\theta_{C}$ $s' = -d\sin\theta_{C} + s\cos\theta_{C}$ where θ_{C} is called the Cabibbo angle.

• With quark mixing, the quark-lepton symmetry applies to doublets like $\begin{pmatrix} u \\ u \end{pmatrix}$ and $\begin{pmatrix} c \\ c \end{pmatrix}$



With the quark mixing hypothesis, some more W-quark vertices are allowed:



where the vertices with quarks within a generation have the coupling constants $g_{ud} = g_{cs} = g_W^{\cos\theta}C$ and the vertices with quarks from different generations have the coupling constants $g_{us} = -g_{cd} = g_W^{\sin\theta}C$

Weak Interactions

Measurements of the Cabibbo angle.

• The Cabibbo angle is not given by the theory but has to be measured e.g. by comparing the decay rates of $\pi^- \rightarrow \mu^- + \bar{\nu}_{\mu}$ with that of $K^- \rightarrow \mu^- + \bar{\nu}_{\mu}$

$$\frac{\Gamma(K^- \to \mu^- \bar{\nu}_{\mu})}{\Gamma(\pi^- \to \mu^- \bar{\nu}_{\mu})} \propto \frac{g_{us}^2}{g_{ud}^2} = \tan^2 \theta_C \quad \text{gives the result} \quad \theta_C = 12.7^\circ \pm 0.1^\circ$$

• When the Cabibbo angle is measured it is also possible to compare the coupling constants within and between generations: $g_W \cos \theta_C = 0,98g_W$

$$g_W \sin \theta_C = 0, 22 g_W$$

• The charmed quark couplings g_{cd} and g_{cs} have been measured in neutrino scattering experiments with the result: $\theta_C = 12^{\circ} \pm 1^{\circ}$

Charmed particle decays.

 Particles with charm quarks almost always give a strange particle in the final state. The reason is that other decays are Cabibbo supressed.



The supression factor is given by:

$$\frac{g_{cd}^2}{g_{cs}^2} = \tan^2 \theta_C = \frac{1}{20}$$
 if $\theta_C = 12, 6^\circ$

Two generation quark mixing can be written in matrix form: $\begin{pmatrix} d'\\ s' \end{pmatrix} = \begin{pmatrix} \cos\theta_C & \sin\theta_C\\ -\sin\theta_C & \cos\theta_C \end{pmatrix} \begin{pmatrix} d\\ s \end{pmatrix}$ with transitions within $\begin{pmatrix} u\\ d' \end{pmatrix}$ and $\begin{pmatrix} c\\ s' \end{pmatrix}$

This means that the following weak transitions are favoured:



 $\begin{pmatrix} \mathbf{t}^{u} \\ \mathbf{t}^{c} \end{pmatrix}$





- The existence of the c-quark was predicted from lepton-quark symmetry before it was discovered in experiments in 1974.
- After the discovery of the τ , v_{τ} and the b-quark, the sixth quark was predicted to complete the symmetry and the top quark was discovered in 1994 with a mass of about 180 GeV/c².
- The third generation gives rise to the Cabibbo-Kobayashi-Maskawa (CKM) matrix $V_{\alpha\beta}$:

$$\begin{pmatrix} d'\\ s'\\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub}\\ V_{cd} & V_{cs} & V_{cb}\\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d\\ s\\ b \end{pmatrix}$$

• The relation between the matrix elements in the CKM-matrix and the coupling constants are given by $g_{\alpha\beta} = g_W V_{\alpha\beta}$ where $\alpha = u,c,t$ and $\beta = d,s,b$.

V. Hedberg

Weak transitions can now take place between:

 $u \leftrightarrow d' = V_{ud}d+V_{us}s+V_{ub}b$ $c \leftrightarrow s' = V_{cd}d+V_{cs}s+V_{cb}b$ $t \leftrightarrow b' = V_{td}d+V_{ts}s+V_{tb}b$

If the mixing between the b and t quarks with lighter quarks can be neglected the CKM-matrix is reduced to:

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} \cos\theta_C & \sin\theta_C & 0 \\ -\sin\theta_C & \cos\theta_C & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

 In reality, this is not correct but V_{ub}, V_{cb}, V_{td} and V_{ts} must be small since otherwise the two-generation mixing model would not agree so well with the data.

b - quarks

- If V_{ub}=V_{cb}=V_{td}=V_{ts}=0 then the t-quark decays to b-quarks 100% of the time but the b-quark cannot decay to lighter quarks i.e. it must be stable. However, experimentally we know that this is not the case.
- Semileptonic decays of the heavy b-quark (mass=4.5 GeV) to the lighter u and c quarks are observed with a decay rate that is proportional to the squared couplings:



$$|g_{ub}|^2 = |V_{ub}|^2 g_W^2$$

b - quarks

The most precise measurements at present give

 $\left|V_{ub}\right| \approx 0,004$ and $\left|V_{cb}\right| \approx 0,04$

This means that the CKM-matrix becomes

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} \cos\theta_C & \sin\theta_C & 0,004 \\ -\sin\theta_C & \cos\theta_C & 0,04 \\ \sim 0 & \sim 0 & \sim 1 \end{pmatrix} \approx \begin{pmatrix} 0,98 & 0,22 & 0,004 \\ -0,22 & 0,98 & 0,04 \\ \sim 0 & \sim 0 & \sim 1 \end{pmatrix}$$

The top quark

- The top quark is much heavier than even the W-bosons and it can decay by $\int W^+$ $\int W^+$
- Since g_{td} and g_{ts} are close to zero, the only significant decay mode of the t-quarks is

 $t \rightarrow W^+ + b$

with a rate proportional to $\alpha_W = g_W^2 / 4\pi \approx 0,0042$

• Estimation of the decay width of the top ($\Gamma \sim \alpha_W m_t \sim 1 \text{ GeV}$) suggests a very short lifetime for this quark:

$$\tau_t \approx 4 \times 10^{-25} s$$

Compare particles decay length

Particle	Lif
W, Z, top	3-4
π⁰ (→ γγ)	0.0
τ	
Charm: D ⁰ /D [±] /D _s	0.4
Bottom: B ⁰ /B ⁺ /B _s /	
K _s (→ ππ)	
κ±	10
π^{\pm}	30
Κ_L (→ πππ)	50
μ (→eν _e ν _μ)	2,0

Lifetime
3-4x10 ⁻¹³ ps
0.3 ps
0.4-1 ps 1
1.5 ps
80 ps
10,000 ps
30,000 ps
50,000 ps
2,000,000 ps

Decay Length 0 0.025µm **90**µm **50-350µm 450µm** 2.7cm 3.7m 7.8m 16 m 659 m

Decay Place Beampipe Beampipe Beampipe Beampipe Beampipe Tracker Tracker No decay No decay No decay

Decay Measurement Not possible Not possible **Microvertex Microvertex** Microvertex Tracker Not possible Not possible Not possible Not possible

The discovery of the top quark

The accelerator: The Tevatron

- The top quark was discovered at the Tevatron accelerator in 1994 in collisions at 1.8 TeV.
- The Tevatron is a superconducting proton-antiproton collider at Fermilab with a length of 6.3 km. It has the same length as SPS but the bending field is 4.5 T compared to 1.8 T and the beam energy can therefore be twice as high.



Weak Interactions

The discovery of the top quark

The accelerator: The Tevatron

• The Tevatron accelerator was put under the old main ring which was used as a pre-accelerator (it has since been removed).





One of the superconducting dipole bending magnets.



A cross section of a dipole magnet showing the coil structure.

Weak Interactions



V. Hedberg

Weak Interactions
The experiment: CDF





The tracker was a drift chamber with thousands of wires parallel to the beams.



The muon detectors were also drift chambers.

V. Hedberg

Weak Interactions

73

Production of top-quarks

In proton-antiproton colliders, pairs of top quarks are mostly produced by the quark-antiquark annihilation process:

 $q + \overline{q} \rightarrow g \rightarrow t + \overline{t}$



The decay of top-quarks

 The most likely decay of a top quark is to a b quark and to a W.



 The W can decay to leptons or hadrons and so the final state is a complex mix of jets and leptons.

$$\begin{array}{c} \longrightarrow & \left\{ \begin{array}{c} l^{-} + \overline{v}_{l} \\ q + \overline{q} \end{array} \right. \\ \longrightarrow & W^{-} + \overline{b} \end{array} \\ \longrightarrow & W^{+} + X \\ \longrightarrow & W^{+} + b \\ & \downarrow \\ & \downarrow \\ q + \overline{q} \end{array}$$

The events that CDF searched for was: $t+t \rightarrow b+l+v+b+q+q$ i) Two b-jets ii) Two light quark jets The signature was iii) A lepton with large transverse energy iv) Missing energy from the neutrino 5 centimeters Tevatron jet #2 *** beam pipe V W b iet #3 t iet #1



 After a selection of likely top event had been made, one could plot the mass distribution of the top-candidates.



The resulting distribution had a large background component but one could nevertheless extract a top mass:

 $M_t = 176 \pm 5 \ GeV$

- The basic vertices with W bosons have:
 - Conserved lepton numbers
 - Not conserved quark flavour (quark mixing)
- The basic vertices with Z bosons have:
 - Conserved lepton numbers
 - Conserved quark flavour (no quark mixing)



In processes in which a photon can be exchanged, a Z⁰ boson can be exchanged as well:



• The reaction $e^+e^- \rightarrow \mu^+\mu^-$ has as an example two dominant contributions:



With simple dimensional arguments one can estimate the crosssection for the photon- and Z-exchange process at low energy:



where E_{cm} is the energy of the colliding electrons and positrons.

- From these formulas one can conclude that the photon exchange process will dominate at low energies.
- However, at E_{cm}=M_z this low-energy approximation fails and the Z⁰ peak is described by the Breit-Wigner formula:

$$\mathbf{\sigma}(E_{CM}) = \frac{M^2}{E_{CM}^2} \left[\frac{C}{\left(E_{CM}^2 - M^2\right)^2 + M^2 \Gamma^2} \right]$$

where M is the mass of the resonance and Γ its decay width.

Weak Interactions



V. Hedberg

- That flavour is conserved at a Z⁰ vertex can be verified by experiments.
- One way of doing this is to study the decay of charged kaons by measuring the decay rate of the following two processes:



 The measured upper limit on the ratio of the decay rate of these two processes was

$$\frac{\sum_{l} \Gamma(K^+ \to \pi^+ + \nu_l + \bar{\nu}_l)}{\Gamma(K^+ \to \pi^0 + \mu^+ + \nu_\mu)} < 10^{-7}$$

until experiment E787 came along

Weak Interactions

 The BNL experiment E787 was a fixed target experiment that used a K⁺ beam created by 24 GeV protons from the AGS accelerator.







V. Hedberg



- The Kaons were stopped in a target made of scintillating fibers and the decay of the K+ at rest was then studied.
- The momentum, energy and range of the particle from the decay was measured.

V. Hedberg

Weak Interactions

• After many years of running two candidate events for $K^+ \rightarrow \pi^+ + v_{l} + \overline{v}_{l}$ were found.



• The result from these two events were:

$$\frac{\sum_{l} \Gamma(K^{+} \to \pi^{+} + \nu_{l} + \bar{\nu}_{l})}{\Gamma(K^{+} \to \pi^{0} + \mu^{+} + \nu_{\mu})} = \frac{1.6 \times 10^{-10}}{0.033} = 5 \times 10^{-9}$$

The events could, however, be explained by second-order charged current reactions rather than neutral current processes:



 Due to the t-d vertex in the third diagram above, it was also possible to set limits on the V_{td} element in the Cabibbo-Kobayashi-Maskawa matrix:

$$0,007 < |V_{td}| < 0,030$$

The Higgs boson

- Generally, experimental data agrees extremly well with the predictions of the gauge invariant electroweak theory.
- However, gauge invariance implies that the gauge bosons have zero mass (if they are the only bosons in the theory). This is true for photons in QED and gluons in QCD but not for W and Z.
- A new scalar field called the Higgs field is introduced to generate mass to the W and Z bosons as well as fermion masses.
- Associated with the field is a new particle called the Higgs boson. The theory predicts how the Higgs boson couples to other particles but not its mass.

The Higgs boson

The Higgs field has the unusual characteristic of having a non-zero value \u00f60 in vacuum (i.e. the field is not zero in its groundstate).



Since the vacuum expectation value is not zero, the vacuum is supposed to be populated with massive Higgs bosons and when a gauge field interacts with the Higgs field it acquires mass.

The Higgs boson

 From the interaction with the Higgs field, the W and Z bosons require masses with the ratio given by

$$\cos\theta_W = \frac{M_W}{M_Z}$$

 In the same way, fermions acquire mass by interacting with the Higgs bosons.

- The coupling constant for this process depends on the fermion mass: $g_{Hff}^2 = \sqrt{2}G_F m_f^2$
- The existance of the Higgs boson has not been experimentally verified despite many years of searches.

V. Hedberg

Weak Interactions

- The LEP project had two phases:
 - LEP 1: The collision energy was equal to the mass of the Z^0 .
 - LEP 2: The collision energy was increased gradually during several years by adding superconducting cavities until it reached its maximum energy (209 GeV).

Higgs search at LEP 1

In this case the Higgs particle would be lighter than the Z⁰ and one should be able to find it in decays of the Z⁰:



• The predicted branching ratio for Higgs production is low $3 \times 10^{-6} \le \frac{\Gamma(Z^0 \to H^0 l^+ l^-)}{\Gamma_{tot}} \le 10^{-4}$

but millions of Z⁰s were produced in the LEP experiments and so the experiments were still sensitive to a Higgs signal.

- The DELPHI experiment looked at one million Z⁰ events and selected those that contained both leptons and hadrons.
- No signal was observed and one concluded that m_H > 56 GeV.



Higgs search at LEP 2

At LEP 2 one expects the main Higgs production to happen by so-called Higgs strahlung:



 Most of the Higgs events would have 4 jets in the final state.
Two of these should be coming from b-quarks.

Example of a Higgs candidate in DELPHI —



V. Hedberg

- During the last year of operation of LEP 2, the ALEPH experiment recorded a couple of events which could be due to the decays of a Higgs boson with a mass of about 115 GeV.
- The other experiments at LEP did not see a signal and when all data was added together there was no discovery.
- The DELPHI experiment put a limit on the Higgs mass of:

 $M_{H} > 114 \text{ GeV/c}^{2}$



The measurement of many electroweak parameters at LEP (and other places) makes it possible to make a global fit with the Higgs mass as a free parameter.



V. Hedberg

The Large Hadron Collider (LHC)

The 27 km long proton-proton collider has a 14 TeV collision energy (575 TeV for lead-lead collisions).



TOILOU

 The 1232 dipole magnets produce a 8.3 Tesla magnetic field which are used to bend the proton trajectory.



The current in the superconducting magnet coils is 11800 Ampere.

The protons are travelling in 2808 bunches that each contain 10¹¹ protons.

- In addition to the dipole bending magnets there are some 386 quadrupole magnets used to focus the protons beams.
- Cavities with strong high-frequency electric fields are used to provide the energy to the beams. The LHC has 2x8 cavities that give 16 MV at 400 MHz.





The ATLAS experiment

ATLAS is the worlds largest particle physics experiment.



V. Hedberg

Weak Interactions

Higgs boson production



V. Hedberg

Higgs boson decay

- There is 10⁹-10¹⁰ inelastic interactions for every Higgs boson that is produced. At low mass most decay to bb and at high mass most decay to WW and ZZ.
- The background is huge and one has to select decays that are are visible above the background (bb are for example hopeless).
- The cleanest process is if the Higgs has a large enough mass so that it can decay to two Z⁰ that then decay to leptons.



 Computer simulations of collisions in which Higgs bosons are detected by finding four



leptons show a very clear signal if the Higgs mass is 300 GeV.





It is possible to use the 4-lepton channel also if m_H < 2m_Z, but then the Higgs decays to one real and one virtual Z⁰.



At a Higgs mass close to the LEP limit, the branching ratio for $H^0 \rightarrow ZZ \rightarrow$ leptons is very small and one is also considering using $H^0 \rightarrow \gamma \gamma$ but this process also has a minute branching ratio: Br = 1-2 x 10⁻³



V. Hedberg

One can estimate the signal significance for different search channels:

